

Math 420, Spring 2016

Second Project: Monday Markov Models

presentation due Tuesday, 3 May, 2016

report due Tuesday, 10 May, 2016

This project explores whether there is benefit in building Markov models that treat the first trading day of the week differently from every other trading day. Consider the following groups of assets.

- (A) This will be the Group A from the first project.
- (B) This will be the Group B from the first project of one of the team members. It will be filled in once the team is assigned.
- (C) This will be the Group C from the first project of one of the team members. It will be filled in once the team is assigned.

For each of the years ending December 31 of the years 2010-2015 use one-year histories of daily returns and uniform weights to calibrate \mathbf{m} and \mathbf{V} . Also use one-year histories of daily return rates and uniform weights to calibrate a Markov model that uses one probability density for the returns on the first trading day of each week, and another probability density for the returns on all other trading days. Because the first trading day of each week is generally a Monday, we will call such models Monday Markov Models.

Find unbiased estimators for the “Monday” return means \mathbf{m}_M and covariances \mathbf{V}_M , as well as the return means \mathbf{m}_O and covariances \mathbf{V}_O for the other trading days. Do you see a “Monday” effect for all assets or some assets? If so, describe it.

Modify the IID model from the lectures into a Markov model that draws returns from a density $p_M(\mathbf{R})$ with means \mathbf{m}_M and covariances \mathbf{V}_M on “Mondays”, and from a density $p_O(\mathbf{R})$ with means \mathbf{m}_O and covariances \mathbf{V}_O on other trading days.

There is a version of the central limit theorem that is more general than the one given in the lectures for IID models which holds for such Markov models. Present this central limit theorem and use it to build an objective function for the Monday Markov Model that is analogous to the one built in the lectures for the IID model depending upon a risk coefficient χ .

Repeat the last homework assignment using both the IID objective function and the Monday Markov objective function with $\chi = 0, .25, .5, .75, 1, 1.25, 1.5, 1.75$ and 2 . Determine which value of χ yields the best performing portfolios in the subsequent year. Describe and explain differences you do or do not find in the performance of the optimal portfolios computed from the IID model and the Monday Markov Model.